

**EXERCISE – II****MULTIPLE CORRECT (OBJECTIVE QUESTIONS)**

1. If  $I = \int_0^{2\pi} \sin^2 x \, dx$ , then

(A)  $I = 2 \int_0^{\pi} \sin^2 x \, dx$  (B)  $I = 4 \int_0^{\pi/2} \sin^2 x \, dx$

(C)  $I = \int_0^{2\pi} \cos^2 x \, dx$  (D)  $I = 8 \int_0^{\pi/4} \sin^2 x \, dx$

2. The value of integral  $\int_0^{\pi} x f(\sin x) \, dx$  is

(A)  $\frac{\pi}{2} \int_0^{\pi} f(\sin x) \, dx$  (B)  $\pi \int_0^{\pi/2} f(\sin x) \, dx$   
(C) 0 (D) None of these

3.  $\int_0^{\infty} \frac{x}{(1+x)(1+x^2)} \, dx$

(A)  $\frac{\pi}{4}$  (B)  $\frac{\pi}{2}$   
(C) is same as  $\int_0^{\infty} \frac{dx}{(1+x)(1+x^2)}$  (D) cannot be evaluated

4. The value of integral  $\int_a^b \frac{|x|}{x} \, dx$ ,  $a < b$  is

(A)  $b - a$  if  $a > 0$  (B)  $a - b$  if  $b < 0$   
(C)  $b + a$  if  $a < 0 < b$  (D)  $|b| - |a|$

5. If  $f(x) = \int_0^x (\cos^4 t + \sin^4 t) \, dt$ ,  $f(x + \pi)$  will be equal to

(A)  $f(x) + f(\pi)$  (B)  $f(x) + 2(\pi)$   
(C)  $f(x) + f\left(\frac{\pi}{2}\right)$  (D)  $f(x) + 2f\left(\frac{\pi}{2}\right)$

6. The value of  $\int_0^1 \frac{2x^2 + 3x + 3}{(x+1)(x^2 + 2x + 2)} \, dx$  is

(A)  $\frac{\pi}{4} + 2 \ln 2 - \tan^{-1} 2$  (B)  $\frac{\pi}{4} + 2 \ln 2 - \tan \frac{1}{3}$   
(C)  $2 \ln 2 - \cot^{-1} 3$  (D)  $-\frac{\pi}{4} + \ln 4 + \cot^{-1} 2$

7. A function  $f(x)$  which satisfies,  $f'(\sin^2 x) = \cos^2 x$  for all real  $x$  &  $f(1) = 1$  is

(A)  $f(x) = x - \frac{x^3}{3} + \frac{1}{3}$  (B)  $f(x) = x^2 - \frac{x}{2} + \frac{1}{2}$   
(C) a polynomial of degree two (D)  $f(0) = 1/2$

8. If  $I_n = \int_0^1 \frac{dx}{(1+x^2)^n}$ ;  $n \in \mathbb{N}$ , then which of the following statements hold good?

(A)  $2n I_{n+1} = 2^{-n} + (2n-1) I_n$  (B)  $I_2 = \frac{\pi}{8} + \frac{1}{4}$   
(C)  $I_2 = \frac{\pi}{8} - \frac{1}{4}$  (D)  $I_3 = \frac{\pi}{16} - \frac{5}{48}$

9. If  $f(x)$  is integrable over  $[1, 2]$ , then  $\int_1^2 f(x) \, dx$  is equal to

(A)  $\lim_{n \rightarrow \infty} \frac{1}{n} \sum_{r=1}^n f\left(\frac{r}{n}\right)$  (B)  $\lim_{n \rightarrow \infty} \frac{1}{n} \sum_{r=n+1}^{2n} f\left(\frac{r}{n}\right)$   
(C)  $\lim_{n \rightarrow \infty} \frac{1}{n} \sum_{r=1}^n f\left(\frac{r+n}{n}\right)$  (D)  $\lim_{n \rightarrow \infty} \frac{1}{n} \sum_{r=1}^{2n} f\left(\frac{r}{n}\right)$

10. If  $f(x) = 2^{\{x\}}$ , where  $\{x\}$  denotes the fractional part of  $x$ . Then which of the following is true?

(A)  $f$  is periodic (B)  $\int_0^1 2^{\{x\}} \, dx = \frac{1}{\ln 2}$   
(C)  $\int_0^1 2^{\{x\}} \, dx = \log_2 e$  (D)  $\int_0^{100} 2^{\{x\}} \, dx = 100 \log_2 e$

11. If  $f(x) = \int_0^x (2 \cos^2 3t + 3 \sin^2 3t) \, dt$ ,  $f(x + \pi)$  is equal to

(A)  $f(x) + f(\pi)$  (B)  $f(x) + 2f\left(\frac{\pi}{2}\right)$   
(C)  $f(x) + 4f\left(\frac{\pi}{4}\right)$  (D) None of these